

# Walking machines: 0-legged-robots

*(only snake-like robots, so far)*

A compilation by [Christian Düntgen](#)

## Pictorial Overview on Crawling Robots



ACM III



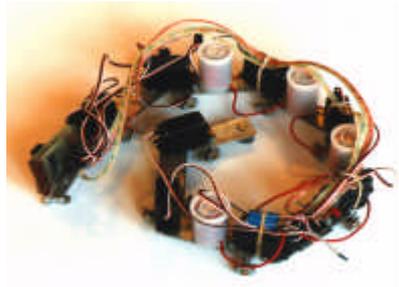
KORYU I



KORYU II



OBLIX



Chabin's snake



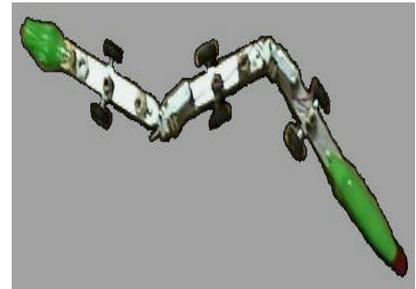
GMD-Snake



GMD-Snake2



JPL-Snake



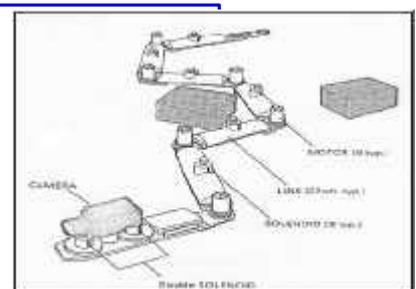
Mita-Lab Snake



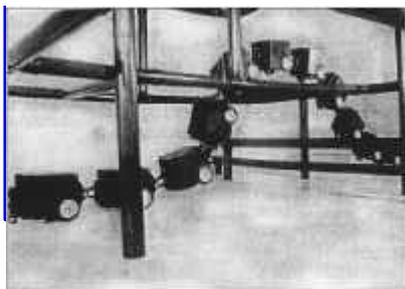
NEC-'Quake'-Snake



Snakey



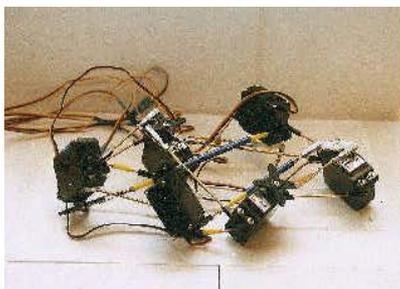
Shan's Snake



ATMS



KAA Snake



'Henrietta'



JHU Metamorphical Robot

## Model

### I. Motivation

Snakes populate wide regions of our planet. They use different methods to move within varying environments (sand, water, solid surface, within trees, ...). They can even climb obstacles and pass rough, smooth and slippery surfaces. Robotic snake might be used to inspect pipes and underground locations or to explore rough territories. As snakes have a lot of degrees of freedoms, their construction pattern is interesting for manipulators e.g. to work with dangerous materials.

Snake-like architectures' high degree of freedoms and allow three-dimensional locomotion and a lot of other tasks as gripping, moving or transporting objects with the body.

Advantages of snake like motion

1. Terrainability  
Snake like robots can traverse rough terrain: they can climb steps whose heights approach its longest linear dimension, pass soft or viscous materials, span gaps, etc.
2. Traction  
Snakes can use almost their full bodylength to apply forces to the ground.
3. Efficiency  
Low costs of body support, no cost of limb motion. But: high friction losses, lateral accelerations of the body.
4. Size  
Small frontal area allows penetration of smaller cross-sectional areas than man-equivalent legged or wheeled vehicles.
5. Redundancy  
Serpentine vehicles consist of many similar segments. The loss of function of some of these may be compensated, though some efficiency will be lost.
6. Sealing  
The surface of a serpentine vehicle is small and does not need to be exposed to the environment in the same way as limbs. This provides advantage to applications in hostile environments.

### Disadvantages of snakelike motion

1. Payload  
Transport of materials is difficult until an integral conduit is used.
2. Degrees of Freedom  
A large number of actuators is necessary. This provides problems to motion planning and control.
3. Thermal Control  
The long stretched form of snakes makes thermal control somehow difficult.
4. Speed  
Robot snakes are far slower than their natural counterparts (reaching speeds up to 3.0 m/s) and far slower than wheeled vehicles.

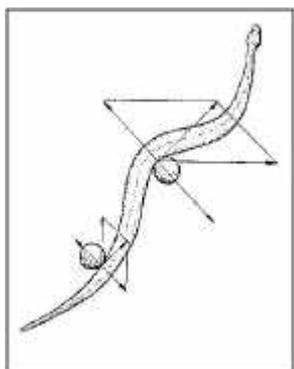
## II. Biological/mathematical model

Snakes use different mechanic principles to move. The most frequent are:

### A. lateral undulation

*"Waves of muscular contraction and relaxation propagate from front to rear. Each point of the body slides along a single track on the ground, without any static contact."* ([Worst '98](#)).

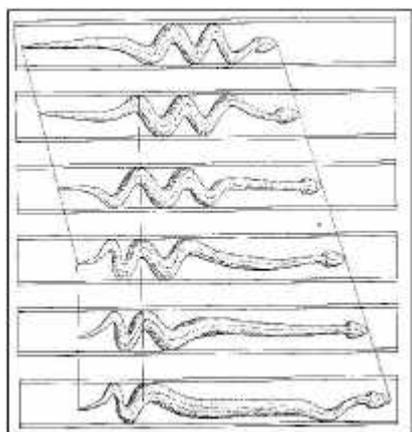
- efficient way to progress
- needs wide space
- does not work on smooth surface
- movement hindered by great body mass



### B. concertina progression

Sequential folding and unfolding of the body used differences in static and dynamic friction along different parts of the body.

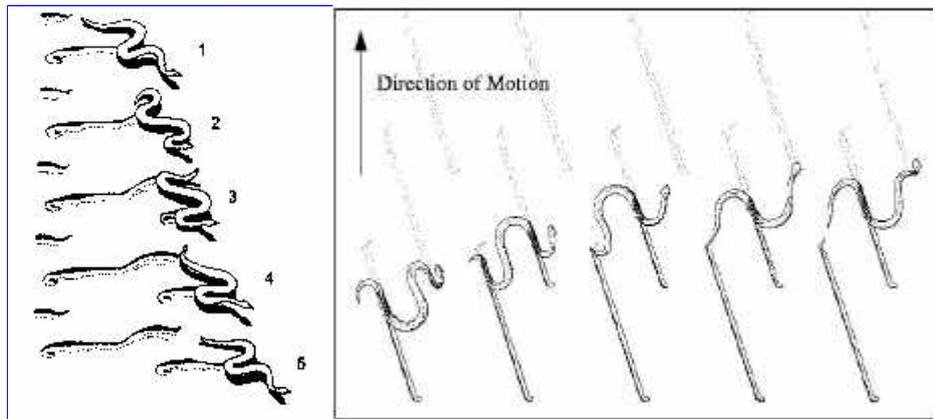
- works even in narrow spaces
- inefficient



### C. sidewinding

Continuous alternating waves of lateral bending while maintaining only two contact points to the ground. Thus, the body is shifted to the side.

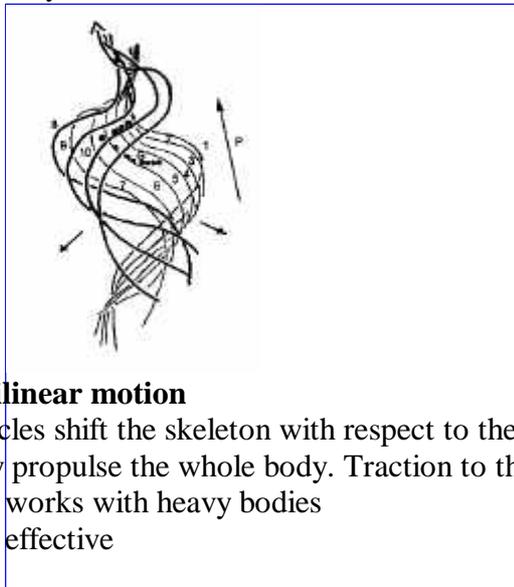
- relatively efficient
- useful on soft grounds
- not in narrow locations



#### D. slide-pushing

Quick waves from head to tail propulse the body as a reaction to slip friction. The belly scales provide the outcome of a forward movement.

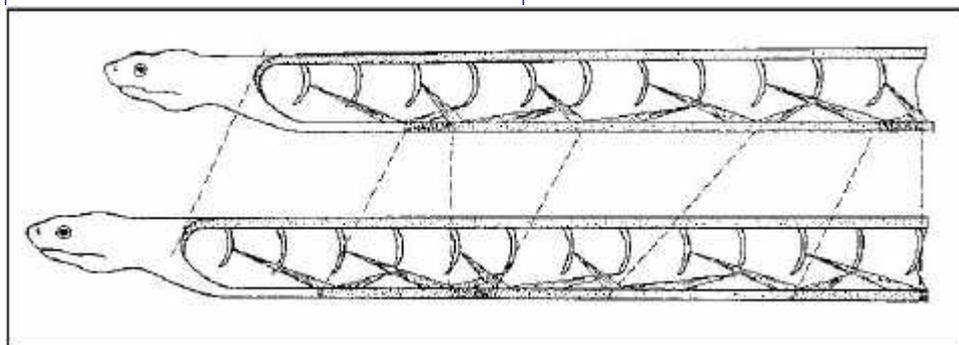
- works on low friction surfaces
- very ineffective



#### E. rectilinear motion

Muscles shift the skeleton with respect to the skin. Waves of muscular contraction along the body propulse the whole body. Traction to the ground is enabled by belly scales.

- works with heavy bodies
- effective



#### F. Other gaits

There are numerous other types of locomotion, e.g.

1. jumping,
2. rolling around the spinal axis,
3. usage of obstacles to push off from,
4. worm-like motion.

By now, robotic snakes implemented all these methods:

1. lateral undulation (A: [ACM III](#)),

2. concertina progression (B: Shan's Snake),
3. sidwinding (C: [GMD-Snake](#)),
4. slide-pushing (D: [Sniky](#)),
5. rectilinear motion (E: Snakey).

### III. Implementation

#### A. Simulation

In most cases, simulators have been used to develop or learn and test programs for the snake's movement. The results of learning on a simulator can be used as a foundation for further learning on the real robot system. Simulators have been used with GMS-Snake, with L. Dowling's snake.

#### B. Hardware

A lot of different serpentine robots have been implemented by now. A [pictorial overview](#) can be found on the top of this page.

## Technology

### I. Controller

Special solutions have to be found to move in a serpentine way. Special problems in controlling serpentine robots are:

1. Uncomplete knowledge  
Under working conditions, a robot has only uncomplete knowledge of its environment. Motion planning must contribute to this aspect.
2. Large number of DOF  
The biggest problem is to cope with the grieving problem of the large number of degrees of freedom (respectively actuators and sensors). Possible solutions are the use of symmetries in motion sequences, distributed control systems, and machine learning techniques.
3. Motion planning  
As serpentine robots do wide lateral motions, a special kind of motion planning is necessary to avoid obstacles and to reach certain destination points. If the vehicle is capable of different gaits, the controller should select the most feasible for its momentary situation. Work on this research area has been done by Choset & Burdick who introduced the Generalized Voronoi Graph (GVG) as a roadmap..

#### A. Motivation

To gain a serpentine movement, the snake robot has to generate sinoid body-motions. Structures used to generate actuator-commands to generate such a kind of movement are:

1. Besselfunctions (Hirose)

Hirose used a combination of trigonometric functions to calculate what he calls a 'serpenoid curve'. This curve is very similar to real snakes' movement and is used to calculate the positions for each joint. The formula used to compute this "backbone curve" follows:

$$x(s) = sJ_0(\alpha) + \frac{4l}{\pi} \sum_{m=1}^{\infty} \frac{(-1)^m}{2m} J_{2m}(\alpha) \sin\left(m\pi \frac{s}{l}\right)$$

$$y(s) = \frac{4l}{\pi} \sum_{m=1}^{\infty} (-1)^{m-1} \frac{J_{2m-1}(\alpha)}{2m-1} \sin\left(\frac{2m-1}{2}\pi \frac{s}{l}\right)$$

2. Fourier

Fourier functions are a primitive way to calculate the joint positions to obtain some

certain backbone curve.

### 3. Parametric curves (Chirikjian)

Polynomial with more than 20 parameters are used to calculate the backbone curve.

### 4. Tables and Masks

For each time step the joint positions are saved in a table. By using masks, a continuous movement can be generated.

To generate more complicated motion patterns, time/joint matrices are used.

## B. Architecture

The easiest way is to adapt the Tables and Masks solution.

In most cases, one main controller is used to determine the robot's general intention and to send commands to the belly sections. Each section is provided with its own controller, which is connected to other segments and to the main controller via a serial bus.

## II. Energy supply

Autonomous power supply is only implemented in few robot snakes (e.g. KAA, PIRAIA, NEC-Quake-Snake). In most cases the energy is provided by a wire connection, thus limiting the snake's range.

Some exemplary data on the GMD-Snake:

- capacity of the battery pack: 47 Wh
- power consumption of built in electronics 20 W, plain motion 25 W, lift of head and 2 sections 40 W

## III. Mechanics

### A. Architecture

Robotic snakes are composed from at least 2 or more similar "belly" modules chained together in some way. In most cases, there are additional "head" or "tail" modules providing special sensors, actuators or power-supplying components. The inter-module connection points may be joints or simply stiff connectors.

Some snakes (ACM) use passive wheels to lessen friction. Others (NEC-Snake) use additional plates that can be used to improve stability in working or spanning situations.

### B. Frame

There are three types of frame prevailing:

1. stiff tubes (OBLIX, NEC Snake, JPL Serpentine Robot, PIRAIA)  
This implements some kind of exoskeleton. It is an easy way to protect the robot's mechanics from external hazards.
2. unframed functional modules ([ACM III](#), KORYU [KR-I](#) & [KR-II](#), Snakey)  
This is somehow working like an endoskeleton and the simplest solution. Protection to the mechanics has to be provided by capsulation of single parts.
3. ribbed structure - eventually bearing some kind of skin - ([GMD-Snake](#))  
This solution is - for my part - the most convenient. It can provide necessary protection to the inner mechanical parts, bear a skin (necessary for some kinds of snakelike motion) and can be built light weighted.

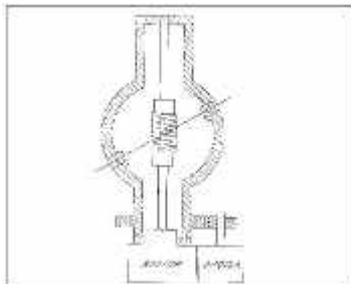
### C. Joints

1. simple joints (1 DOF)  
Simple joints are used to allow a robot to bend into horizontal or vertical direction. They are easy to control and very cheap.
2. ball-and-socket (2 DOF)  
Mostly used in architectures that use stiff tubes as a frame for the robot. Ball-and-socket joints are somehow difficult to be controlled with actuators. There are some approaches to construct special-purpose joints for use within robot snakes. They are somewhat expensive but allow the connected modules to act mostly independent from each other.
3. flexible connection (2 DOF)

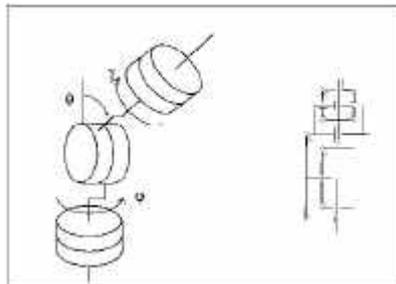
Flexible connection can be implemented by using rubber or other elastic material that can be bend easy in any direction. This is used in GMD-Snake. It is easy to use in a combination with string-and-winch actuators.

#### 4. special joints

big efforts are made to develop special purpose joints for robotic snakes, that provide up to 3 DOF.



rotating joint  
[Ikeda/Takanashi]



NEC-Snake's joint



PIRAIA-joint

## IV. Sensors

### A. Tactile sensors

Bumpers are used to sense contact to the ground and solid obstacles.

### B. Light sensors

Light sensors are used to measure distances to obstacles or to calculate some direction to creep to. In most cases, they are placed within the snake's "head"-module.

### C. Joint-position sensors

Special sensors are used to inform the robot of the positions and bending of it's joints. This sensors may consist of potentiometers, tension-sensors, reed contacts, revolution-counters, ... Joint-position sensors are needed for each degree of freedom.

## V. Actuators

Snake like robots should not use driving wheels for moving, but bending and stretching or other forms of changing their form (as described before). To achieve these motions, different types of actuators are used, almost all are powered by Electro-magnetic motors (e.g. servos):

### A. motor-lever actuators

A motor is shifting a lever transmitting its force, e.g. to bend a joint.

### B. motor-direct actuators

A motor is directly connected to a part to be rotated around the motor's axis.

### C. string-and-winch actuators

A motor drives a winch to control the length of a string. Thus the string can be used to bend a joint. This mechanism drives the GMD-Snake.

However, some snake robots ([GMD Snake2](#)) use driving wheels to move. This allows for higher velocities and allows the snake to locomote much faster.

## VI. Skin

Serpentine robots make essential use of their bodies' friction. Additionally, for some gaits specially structured surfaces are required, that emulate the functions of a real snake's scales (this

is providing a higher friction to backward movements of the body, but a low friction to forward motions). The skin has to be elastic to accommodate the body's movements. So, development of adequate skins for robot snakes seems to be useful.

## Applications

- bridge inspection, inspection of pipe systems (e.g. Kaa snake, GMD Snake2)
- minimally invasive surgery
- search & rescue, e.g. in collapsed buildings (e.g. NEC-Quake snake)
- elephant-trunk-like manipulators

## Literature

### I. List of papers and books on snake like robotics

1. Yoji Umetani and Shigeo Hirose,  
*Biomechanical study of actice cord-mechanism with tactile sensors*,  
In Proc. 6th Int. Symp. On Industrial Robots, pp. c1-1-c1-10, Nottingham, 1976.
2. Shigeo Hirose and Yoji Umetani,  
*An actice chord mechanism with oblique swivel joints and its control*,  
In Proc. 4th RoManSy Symp., pp. 327-340, Zaborow/Poland, 1981, PWN-Polish Scientific Publishers.
3. K. Asano,  
*Control System for a Multihoint Inspection Robot*,  
Poc. of the 1984 Topical Meeting on Robotics and Remote Handling in Hostile Environments, Gatlinburg/Tenn., pp 375-382, 1984.
4. Shigeo Hirose,  
*Connected differential mechanism and its applications*,  
In Proc. 2nd Int. Conf. On Advanced Research, pp. 319-326, 1985.
5. Shigeo Hirose and Akio Morishima,  
*Articulated body mobile robot*,  
In Proc. 7th RoManSy Symp., pp. 1-8, Hermes, 1988.
6. Shigeo Hirose and Akio Morishima,  
*Design and control of a mobile robot with an articulated body*,  
The Int. J. Robotics Research, 9(2):99, 1990.
7. Shigeo Hirose,  
*Three basic types of locomotion in mobile robots*.  
In Proc. 5th Int. Conf. Advanced Robots, pp. 12-17, Pisa/Italy, 1991.
8. Shigeo Hirose, Akio Morishima, and Siniti Tukagosi,  
*Design of practical snake vevikel: Articulated body mobile robot KR-II*,  
In Proc. 5th Int. Conf. Advanced Robotics, pp. 833-838, Pisa/Italy, 1991.
9. G. S. Chirikjian and J. W. Burdick,  
*Design, implementation, and experiments with a thirty-degree-of-freedom 'hyper-redundant' robot*.  
In ISRAM 1992, November 1992.
10. Shigeo Hirose and Shinichi Amano,  
*The VUTON: High payload high efficiency holonomic omni-directional vehicle*,  
In Proc. Int. Symp. On Robotics Research, pp. 253-260, 1993.
11. Shigeo Hirose and Akio Morishima,  
*Impedance control of articulated body mobile robot "Koryu"*,  
In Proc. IEEE/RSJ Int. Conf. On Intelligent Robots and Systems, pp. 1786-1790, 1993.

12. K. Asano et al.,  
***Multijoint Inspection Robot***,  
IEEE Transactin on Industrial Electronocs, Vol. IE-30, No. 3, pp. 277-281,1993.
13. Shigeo Hirose,  
***Biologically Inspired Robots: Snake-like Locomotors and Manipulators***,  
Oxford University Press, 1993. ISBN 0-19-856261-6.
14. Y. Shan et al.,  
***Design and Motion Planning of a Mechanical Snake***,  
IEEE Transactions on Systems, Man, and Cybernetics, Vol. 23(4), pp. 1091-1100, 1993.
15. Lee, T., Ohm, T., and Hayati, S.,  
***A Highly Redundant Robot System for Inspection***,  
Proceedings of the Conference on Intelligent Robotics in the Field, Factory, Service, and Space (CIRFFSS '94), Houston, Texas, March 21-24, 1994, pp. 142-149.
16. G. S. Chirikjian, and J. W. Burdick,  
***Kinematics of Hyper-Redundant Robot Locomotion***,  
IEEE Transactions on Robotics and Automation, Vol. 11(6), pp. 781-793, 1995.
17. J. W. Burdick, J. Radford, G. S. Chirikjian,  
***A Sidewinding Locomotion Gait for Hyper-Redundant Robots***,  
Advanced Robotics, Vol. 9(3), pp. 195-216, 1995.
18. R. Desai, C. J. Rosenberg, J. L. Jones,  
***Kaa: An Autonomous Serpentine Robot Utilizes Behavior Control***,  
1995 Int. Conf. on Intelligent Robots and Systems, IROS'95, Pittsburgh/PA, Vol. 3 pp. 250-255, 1995.
19. H. Choset and J. Burdick,  
**[Sensor Based Planning, Part I: The Generalised Voronoi Graph](#)**,  
Proc. IEEE Int. Conf. on Robotics and Automation, 1995.
20. H. Choset and J. Burdick,  
**[Sensor Based Planning, Part II: Incremental Construction of the Generalized Voronoi Graph](#)**,  
Proc. IEEE Int. Conf. on Robotics and Automation, 1995.
21. N. Takanashi, H. Choset and J. Burdick,  
**[Experimental Results of Sensor Based Planning for hyper-redundant Manipulators](#)**,  
???
22. H. Choset and J. Burdick,  
**[Sensor Based Planning and Nonsmooth Analysis](#)**,  
IEEE/ICRA, San Diego, California, 1994.
23. H. Choset, J. Burdick,  
**[Extensibility in Local Sensor Based Planning for Hyper-redundant Manipulators \(Robot Snakes\)](#)**,  
???
24. H. Choset, W. Henning,,  
**[A Follow-The-Leader Approach to Serpentine Robot Motion Planning](#)**,  
???
25. W. Henning, Frank Hickman, H. Choset,  
**[Motion Planning for Serpentine Robots](#)**,  
???
26. J. P. Ostrowski and J. W. Burdick,  
**[Gait kinematics for a serpentine robot](#)**,  
In Int. Conf. On Robotics and Automation, 1996.
27. H. Choset and J. Burdick,  
***Sensor Based Motion Plannig: The Hierarchical Generalized Voronoi Graph***,  
Workshop on Algorithmic Foundations of Robotics, 1996.
28. H. Choset,

- Sensor Based Motion Planning: The Hierarchical Generalized Voronoi Graph*,  
Ph.D. Thesis, Caltech, 1996.
29. K. L. Paap, M. Dehlwisch, B. Klaassen, 1995.  
[GMD-Snake: A Semi-Autonomous Snake-like Robot](#),  
In: Distributed Autonomous Robotic Systems 2, Springer-Verlag, Tokyo, 1996.  
Description of the GMD-Snake's physical architecture.
  30. R. Worst, R. Linnemann,  
[Construction and Operation of a Snake-like Robot](#),  
IEEE International Joint Symposia on Intelligence and Systems, 1996.  
Description of the GMD-Snake's controller/program structure.
  31. M. Nielsson,  
*Ripple and Roll: Slip-free Snake Robot Locomotion*,  
Proc. Mechatronic Computing for Perception and Action (MCPA'97), Pisa/Italy, 1997
  32. M. Nielsson,  
*Snake Robot Free Climbing*,  
Int. Conf. on Robotics and Automation (ICRA'97), Albuquerque/NM, 1997.
  33. R. Worst,  
*Robotic Snakes*,  
3rd. German Workshop on Artificial Life, Veral Haary Deutsch, Frankfurt/Main, 1998.  
A short but useful overview on robotic snakes.
  34. Kevin Dowling,  
*Terrestrial locomotion without wheels or legs*,  
A Thesis Proposal The Robotics Intitute, Carnegie Mellon, Pittsburgh, PA.
  35. K. Dowling,  
[Limbless Locomotion: Learning to Crawl with a Snake Robot](#),  
doctoral dissertation, tech. report CMU-RI-TR-97-48, Robotics Institute, Carnegie Mellon  
University, December 1997.

## II. Links to collections of electronically available papers

- A good collection on different robotic-related papers can be found at  
<http://robby.caltech.edu/papers.html>.
- Additional papers related to the GMD-Snakes can be found at  
<http://borneo.gmd.de/RS/snake/>.

## III. List of papers and books on Hyper-Redundant Manipulators and Mobile Robots

1. G. S. Chirikjian, Hyper-Redundant Manipulator Dynamics:  
*A Continuum Approximation, Advanced*  
Robotics, pp217-243, Vol. 9, No. 3, 1995.
2. G. S. Chirikjian, and J. W. Burdick,  
*Kinematically Optimal Hyper-Redundant Manipulator Configurations*,  
IEEE Transactions on Robotics and Automation, pp794-806, Vol. 11, 1995.
3. G. S. Chirikjian, and J. W. Burdick,  
*A Hyper-Redundant Manipulator, IEEE Robotics and Automation*  
Magazine, pp22-29, December 1994.
4. G. S. Chirikjian, and J. W. Burdick,  
*A Modal Approach to Hyper-Redundant Manipulator Kinematics*,  
IEEE Transactions on Robotics and Automation, pp343-354, Vol. 10, 1994.
5. G. S. Chirikjian, and J. W. Burdick,

- A Geometric Approach to Hyper-Redundant Manipulator Obstacle Avoidance*,  
ASME Journal of Mechanical Design, pp580-585, Vol. 114, December 1992.
6. S. Ma, D. N. Nenchev, and S. Hirose:  
*Improving Local Torque Optimization Techniques for Redundant Robotic Mechanisms*,  
Int. J. of Robotic Systems, 8-1, 1991, 79---91
  7. S. Ma, S. Hirose, and H. Yoshinada:  
*Design and Experiments for a Coupled Tendon-driven Manipulator*,  
IEEE Control Systems Magazine, 13-1, 1993, 30---36
  8. S. Ma, S. Hirose, and H. Yoshinada:  
*Development of a Hyper-redundant Multijoint Manipulator for Maintenance of Nuclear Reactors*,  
Int. J. of Advanced Robotics, 9-3, 1995, 281---300
  9. S. Ma and D. N. Nenchev:  
*Local Torque Minimization for Redundant Manipulators: A Correct Formulation*,  
Int. J. of Robotica, 14-2, 1996, 235---239
  10. S. Ma and S. Hirose:  
*Dynamic Redundancy Resolution of Redundant Manipulators with Local Optimization of a Kinematic Criterion*,  
Int. J. of Advanced Robotics, 10-1, 1996, 65---80
  11. S. Ma:  
*A New Formulation Technique for Local Torque Optimization of Redundant Manipulators*,  
IEEE Trans. on Industrial Electronics, 43-4, 1996, 462---468
  12. S. Ma:  
*A Balancing Technique to Stabilize Local Torque Optimization Solution of Redundant Manipulators*,  
Int. J. of Robotic Systems, 13-3, 177---185, 1996
  13. S. Ma and S. Hirose:  
*A Dynamic Approach to Realtime Obstacle Avoidance Control of Redundant Manipulators*,  
JSME Int. J., Series C: Dynamics, Control, Robotics, Design and Manufacturing, 39-2C, 1996, 317---322
  14. S. Ma:  
*Local Torque Minimization of Redundant Manipulators with Considering End-Motion Joint Velocities*,  
IASTED Int. J. of Robotics and Automation, 12-2, 1997, 65---70
  15. S. Hirose and S. Ma:  
*Redundancy Decomposition Control for Multijoint Manipulator*,  
in Proc. 1989 IEEE Int. Conf. on Robotics and Automation, 1, 1989, 119---124
  16. S. Hirose and S. Ma:  
*Moray Drive for Multijoint Manipulator*,  
in Proc. 5th Int. Conf. on Advanced Robotics, 1, 1991, 521---527
  17. S. Hirose and S. Ma:  
*Coupled Tendon-driven Multijoint Manipulator*,  
in Proc. 1991 IEEE Int. Conf. on Robotics and Automation, 2, 1991, 1268---1275
  18. S. Ma, S. Hirose, H. Yoshinada, and T. Yamazaki:  
*Development of Coupled Tendon-driven Multijoint Manipulator*,  
in Proc. 1991 Int. Workshop on Intelligent Robots and Systems (IROS'91), 2, 1991, 725---730
  19. S. Ma, S. Hirose, and H. Yoshinada:  
*CT ARM-I: Coupled Tendon-driven Multijoint Manipulator Model I; --- Design and Basic Experiments ---*,  
in Proc. 1992 IEEE Int. Conf. on Robotics and Automation, 3, 1992, 2094---2100

20. S. Hirose, K. Yokoshima, and S. Ma:  
***2-DOF Moray Drive for Super-Redundant Manipulators,***  
in Proc. 1992 Int. Conf. on Intelligent Robots and Systems (IROS'92), 3, 1992,  
1735---1740B
21. S. Ma and S. Hirose:  
***Dynamic Redundancy Resolution of Redundant Manipulators with Local Optimization of a Kinematic Criterion,***  
in Proc. 2nd Asian Conf. on Robotics and Its Application, 1994, 236---243
22. S. Ma and S. Hirose:  
***A Dynamic Approach to Real-time Obstacle Avoidance Control of Redundant Manipulators,***  
in Proc. 1994 JSME Spring Annual Meeting (International Session), IV, 1994, 430---432
23. S. Ma, S. Hackwood, and G. Beni:  
***Multi-Agent Supporting System (MASS): Control with Centralized Estimator of Disturbance,***  
in Proc. 1994 Int. Conf. on Intelligent Robots and Systems (IROS'94), 1, 1994, 679---686
24. S. Ma:  
***Local Torque Optimization of Redundant Manipulators in Torque-Based Formulation,***  
in Proc. 1994 IEEE Int. Conf. on Industrial Electronics (IECON '94), 2, 1994, 697---702
25. S. Ma and S. Hirose:  
***Development of a Super-redundant Multijoint Manipulator for Maintenance of Nuclear Reactors,***  
in Proc. 1994 Specialists Meeting on Application of AI and Robotics to Nuclear Plants,  
1994, 131---142
26. S. Ma:  
***A Stabilized Local Torque Optimization for Redundant Manipulators,***  
in Proc. 1995 IEEE Int. Conf. on Robotics and Automation, 3, 1995, 2791---2796
27. S. Ma and D. N. Nenchev:  
***Local Torque Minimization for Redundant Manipulators: A Correct Formulation,***  
in Proc. 7th Int. Conf. on Advanced Robotics, 2, 1995, 645---650
28. S. Ma:  
***Real-time Algorithm for Quasi-Minimum Energy Control of Robotic Manipulators,***  
in Proc. 1995 IEEE Int. Conf. on Industrial Electronics (IECON '95), 2, 1995, 1324---1329
29. S. Ma:  
***Local Torque Minimization of Redundant Manipulators with Considering End-Motion Joint Velocities,***  
in Proc. 1996 IEEE Int. Conf. on Systems, Man, and Cybernetics (SMC'96), 2, 1996,  
1477---1482
30. D. N. Nenchev, Y. Tsumaki, S. Ma, and M. Uchiyama:  
***Singularity-Consistent Dynamic Path Tracking Under Torque Limits,***  
in Proc. 1996 Int. Conf. on Intelligent Robots and Systems (IROS'96), 1, 1996, 590---595
31. S. Ma and M. Konno:  
***An Obstacle Avoidance Scheme for Hyper-Redundant Manipulators --- Global Motion Planning in Posture Space ---,***  
in Proc. 1997 IEEE Int. Conf. on Robotics and Automation (ICRA'97), 1, 1997, 161---167
32. S. Ma:  
***Dynamic Control Approach for a Coupled Tendon-driven Manipulator,***  
in Proc. 3rd Asian Conf. on Robotics and Its Application, 1997, 365---370
33. S. Ma and I. Kobayashi:  
***Obstacle Avoidance Control of Multijoint Manipulator via 2-DOF Moray Drive Control,***  
  
in Proc. 3rd Asian Conf. on Robotics and Its Application, 1997, 329---334
34. A. Naito and S. Ma:

- Analysis of the Creeping Locomotion of Snake-like Robots*,  
in Proc. 3rd Asian Conf. on Robotics and Its Application, 1997, 393---398
35. S. Ma and I. Kobayashi:  
*An Obstacle Avoidance Control Scheme for the "Moray Arm" on Basis of Posture Space Analysis*,  
in Proc. 1998 Symp. on Image, Speech, Signal Processing, and Robotics (ISSPR'98), 1998, 363---368
36. S. Ma:  
*Simulation of Snake-like Robot Creeping Locomotion Adapted to Environment*,  
in Proc. 1999 TITech COE/Super Mechano-Systems Workshop (SMS'99), 1999, 94---103
37. S. Ma:  
*Analysis of Snake Movement Forms for Realization of Snake-like Robots*,  
in Proc. 1999 IEEE Int. Conf. on Robotics and Automation (ICRA'99), 1999
38. S. Ma, D. N. Nenchev, and S. Hirose:  
*Improving Local Torque Optimization Techniques for Redundant Robotic Mechanisms*,  
in Proc. 1989 Annual Conf. of the Robotics Society of Japan, 2, 1989, 653---656
39. S. Ma, S. Hockwood, and G. Beni:  
*Multi-Agent Supporting Systems (MASS): Control with Centralized Estimator of Disturbance*,  
in Proc. 1993 Annual Conf. of the Robotics Society of Japan, 1, 1993, 111---114
40. S. Ma and S. Hirose:  
*A New and Efficient Method for the Pseudoinverse of Underdetermined Matrices*,  
in Proc. 1993 Annual Conf. of the Robotics Society of Japan, 3, 1993, 1145---1148
41. S. Ma and S. Hirose:  
*A New and Efficient Method for the General Solution of Underdetermined Linear Systems*,  
in Proc. 1993 Annual Conf. of the Robotics Society of Japan, 3, 1993, 1149---1152
42. S. Ma:  
*Quasi-Minimum Energy Trajectory Planning for Robotic Manipulators*,  
in Proc. 1994 Annual Conf. of the Robotics Society of Japan, 3 1994, 871---872

#### IV. List of papers and books on Metamorphic and Amoeba- like Robots

1. Amit Pamecha, Imme Ebert-Uphoff, Gregory S. Chirikjian,  
[\*Useful Metrics for Modular Robot Motion Planning\*](#),  
IEEE Transactions on Robots and Automation, pp531-545, Vol.13, No.4, August 1997.
2. Gregory Chirikjian, Amit Pamecha, Imme Ebert-Uphoff,  
[\*Evaluating Efficiency of Self-Reconfiguration in a Class of Modular Robots\*](#),  
Journal of Robotic Systems, pp317-338, Vol.13, No.5, 1996.
3. Pamecha, A.,Chiang, C., Stein, D., Chirikjian, G.S.,  
[\*Design and Implementation of Metamorphic Robots\*](#),  
Proceedings of the 1996 ASME Design Engineering Technical Conference and Computers in Engineering Conference, Irvine, California, August 1996.
4. Chirikjian G.S.,Pamecha A.,  
[\*Bounds for Self reconfiguration of Metamorphic Robots\*](#),  
JHU Technical Report, RMS-9-95-1.
5. Richard Mason and Joel W. Burdick,  
[\*Propulsion and Control of Deformable Bodies in an Ideal Fluid\*](#),  
1999 IEEE International. Conference on Robotics and Automation (to appear).
6. Pamecha A.,Chirikjian G.S.,  
[\*A Useful Metric for Modular Robot Motion Planning\*](#),  
JHU Technical Report, RMS-9-95-2.
7. Chirikjian G.S.,

- [Kinematics of a Metamorphic Robotic System](#),  
IEEE International Conference on Robotics and Automation, pp449-455, May 1994.
8. Peter Dittrich, Andre Skusa, Wolfgang Kantschik, and Wolfgang Banzhaf,  
[Dynamical Properties of the Fitness Landscape of a GP Controlled Random Morphology Robot](#)  
GECCO'99, Orlando, 1999.
  9. Peter Dittrich, Andreas Buerger and Wolfgang Banzhaf,  
[Random Morphology Robot - A Test Platform for Online Evolution](#)  
Robotics and Autonomous Systems (submitted), 1999.
  10. Peter Dittrich, Andreas Buerger and Wolfgang Banzhaf,  
[Learning to Move a Robot with Random Morphology](#)  
In: Evolutionary Robotics, First European Workshop, EvoRob98, Paris, France, April 1998, Proceedings, Phil Husbands and Jean-Arcady Meyer (eds.), LNCS 1468, pp. 165-178 Springer, Berlin, 1998.
  11. Andreas Buerger,  
*Zwei mechanische Systeme lernen "Laufen"*  
Diploma thesis at the CS-department at University of Dortmund, Dortmund, 1997.

## Links

### I. To the project

<http://www.cybercomm.net/~alindsey/rw97/snake.html><http://mozu.mes.titech.ac.jp/research/snake/>

Information on different snakelike robots and manipulators at Hirose & Yoneda Labs

<http://mozu.mes.titech.ac.jp/research/snake/acm3/acm3.html>

Active Code Mechanism No.3 (ACM III) (1972-1975)

First artificial serpentine movement.

<http://mozu.mes.titech.ac.jp/research/snake/kr2/kr2.html>

Articulated Body Mobile Robot KORYU II (KR-II) (1989)

<http://mozu.mes.titech.ac.jp/research/snake/kr1/kr1.html>

Articulated Body Mobile Robot KORYU I (KR-I) (1985-1992)

<http://borneo.gmd.de/RS/snake/>

GMD Snake - Robot (1996)

<http://ais.gmd.de/BAR/snake2.html>

GMD Snake2 - Robot (1998-)

<http://borneo.gmd.de/~worst/snake-collection.html>

Link-Collection

<http://www.sics.se/piraia/>

PIRAIA-Project at the Swedish Institute of Computer Science, including a snake robot

<http://www.ctrl.titech.ac.jp/ctrl-labs/mita-lab/snake/>

First approaches to a new robot snake...

<http://kamine.dse.ibaraki.ac.jp/~shugen/snakeE.html>

Analysis of Snake Movement and Development of Snake-like Robot  
Only few informations, by now...

<http://www.gmd.de/FIT/KI/CogRob/Projects/Makro/makro.html>

Snakelike multi-segmented wheel driven robot

<http://robby.caltech.edu/~chen/res-medical.html>

Snakelike robot-micro-endoscope

[http://agip.sciences.univ-metz.fr/~mihalach/Copernicus\\_projet\\_engl.html](http://agip.sciences.univ-metz.fr/~mihalach/Copernicus_projet_engl.html)

Snake-like Flexible Micro-robot (1995-)

[http://ourworld.compuserve.com/homepages/laurent\\_chabin/snake.htm](http://ourworld.compuserve.com/homepages/laurent_chabin/snake.htm)

Sniky - A Mechanical Snake (1994-1995)

<http://mozu.mes.titech.ac.jp/research/snake/snake.html>

Overview on different snakelike robots

<http://mozu.mes.titech.ac.jp/research/snake/snake.html>

Biomechanics of the snakes

[http://ourworld.compuserve.com/homepages/laurent\\_chabin/slither.htm](http://ourworld.compuserve.com/homepages/laurent_chabin/slither.htm)

How Snakes Walk

[http://ourworld.compuserve.com/homepages/laurent\\_chabin/insects.htm](http://ourworld.compuserve.com/homepages/laurent_chabin/insects.htm)

Insectlike, snakelike, ... robots

<http://robby.caltech.edu/papers.html>

Some papers on Sensor Based Planning, Robot Locomation, etc.

<http://robotics.jpl.nasa.gov/tasks/rsi/accomplishments/snake/snake.html>

JPL-Serpentine Robot for visual inspection

<http://httpsrv.ocs.drexel.edu/~st93yjl/SDP/HTML/fphtml/fpaper.html>

Semi-Autonomous Snake-Like Robot

<http://www.cybercomm.net/~alindsey/rw97/snake.html>

Snake - a combatant at Robot Wars 97

## II. To related websites

### A. Hyper-redundant manipulators

1. <http://mozu.mes.titech.ac.jp/research/snake/oblique/oblique.html>  
OBLIX and MOGURA - snakelike hyper-redundant arms (1978-79, 1982-84)
2. <http://mozu.mes.titech.ac.jp/research/snake/endscope/endscope.html>  
ELASTOR - Shape Memory Alloy Robot (1980-1986)
3. <http://mozu.mes.titech.ac.jp/research/snake/sg/sg.html>  
Soft Gripper I, II, III (SG I, II, III) (1976-1984)
4. <http://robby.caltech.edu/~chen/res-medical.html>  
snakelike robot-endoscope

5. <http://uirvli.ai.uiuc.edu/tlewis/pics/snake.html>

R7 - a snakelike manipulator (late 1980's)

## B. Morphologic robots

1. <http://caesar.me.jhu.edu/metamorphic.html>  
metamorphic robot
2. <http://www.sics.se/~ojala/protozoa.shtml>  
Protozoa inspired robot control (1995)
3. <http://ls11-www.cs.uni-dortmund.de/alife/rmrobot>  
Random Morphology Robot "Henrietta" (1997-)

## C. Other forms of non-legged locomotion

1. <http://mdesign.os.u-tokai.ac.jp/katolab/katolabe.html>  
underwater robots
2. <http://robotics.eecs.berkeley.edu/~koo/bear.html>  
BEAR-Berkeley Aerobot (Autonomous Helicopter) (1996-)

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# Notes

<ftp://publications.ai.mit.edu/ai-publications/1000-1499/AIM-1126.ps>

Twilight Zones and Cornerstones: A Gnat Robot Double Feature